

P-151/002 Random Graded HWK

Total Pts = 75

8-23 $F = 55 \text{ N}$, $b = 74 \text{ cm} \left(\frac{1 \text{ m}}{100 \text{ cm}} \right) = 0.74 \text{ m}$, $\theta = 90^\circ$

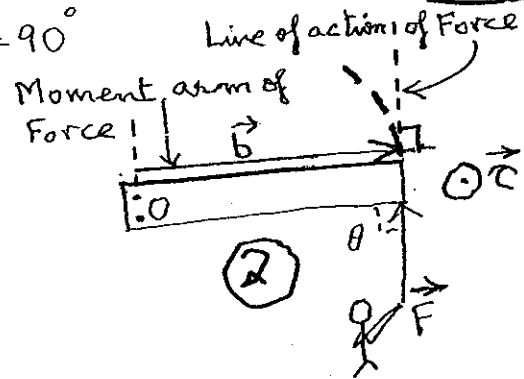
10 (a) $\vec{\tau} = \vec{r} \times \vec{F} = bF \sin \theta = bF = 0.74 \text{ m} \times 55 \text{ N}$

$\Rightarrow \tau = 40.7 \text{ Nm}$ (4)

(b) For $\theta = 45^\circ$

$\tau = 0.74 \text{ m} \times 55 \text{ N} \sin 45^\circ = \frac{40.7 \text{ Nm}}{\sqrt{2}}$

$L = 28.78 \text{ Nm}$ (4)

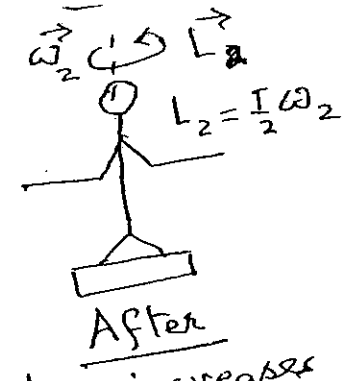
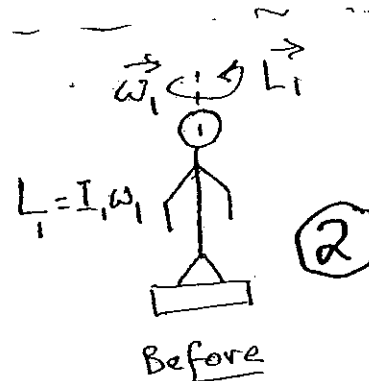


15 8-53 $\omega_1 = 1.3 \frac{\text{rev}}{\text{s}} \left(\frac{2\pi \text{ rads}}{1 \text{ rev}} \right)$

$L = 2.6\pi \frac{\text{rads}}{\text{s}}$ (2)

$\omega_2 = 0.8 \frac{\text{rev}}{\text{s}} \left(\frac{2\pi \text{ rads}}{1 \text{ rev}} \right)$

$L = 1.6\pi \frac{\text{rads}}{\text{s}}$ (2)



(a) When arms are raised the moment of inertia increases

$\Rightarrow I_2 > I_1$. However, angular momentum is conserved since no external torque is applied to the system $\Rightarrow L_2 = L_1 \Rightarrow I_2 \omega_2 = I_1 \omega_1$
 Since $I_2 > I_1$, we must have $\omega_2 < \omega_1$ (4)

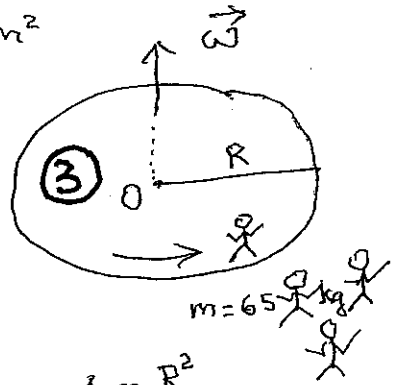
(b) $\frac{I_2}{I_1} = \frac{\omega_1}{\omega_2} = \frac{2.6\pi \text{ rads/s}}{1.6\pi \text{ rads/s}}$

$L = 1.63$ (5)

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15 8-62 $R = \frac{4.2 \text{ m}}{2} = 2.1 \text{ m}$, $\omega = 0.8 \frac{\text{rads}}{\text{s}}$, $I = 1760 \text{ kg m}^2$

The angular momentum of merry-go-round plus people will be conserved since no external torque is applied to the system.



$L_f = L_i \Rightarrow I_i \omega_i = I_f \omega_f$ (2)

$\Rightarrow \omega_f = \frac{\omega_i I_i}{I_f} = \omega_i \frac{I_{mgr}}{I_{mgr} + I_{people}}$ where $I_{people} = 4mR^2$

$\omega_f = \frac{0.8 \left(\frac{\text{rads}}{\text{s}} \right) \times 1760 \text{ kg m}^2}{1760 \text{ kg m}^2 + 4(65 \text{ kg})(2.1 \text{ m})^2}$

$\omega_f = \frac{1408 \text{ rads/s}}{1760 + 1146.6}$

$\omega_f = \frac{1408 \text{ rads}}{2906.6 \text{ s}}$

(a) $\omega_f = 0.48 \frac{\text{rads}}{\text{s}}$ (5)

(b) If 4 people were on merry-go-round initially and they jump off radially outward from merry-go-round, they would exert no torque on the merry-go-round!

(5) So merry-go-round would continue to have an angular speed of $0.8 \frac{\text{rads}}{\text{s}}$