

HW Solution

24.52 & 24.66

24.52 (a) $C_0 = \epsilon_0 \frac{A}{d}$

$$k = \frac{C}{C_0} \quad C = kC_0 = k\epsilon_0 \frac{A}{d}$$

$$\frac{C}{A} = \frac{k\epsilon_0}{d} = \frac{10 \times 8.85 \times 10^{-12}}{7.5 \times 10^{-9}} = 1.18 \times 10^{-2} \text{ F/m}^2$$

(b) $E = \frac{V}{d} = \frac{85 \text{ mV}}{7.5 \text{ nm}} = \frac{8.5 \times 10^{-2} \text{ V}}{7.5 \times 10^{-9} \text{ m}} = 1.13 \times 10^7 \text{ V/m}$

24.66 (a) $\frac{1}{C_{\text{eff}}} = \frac{1}{C_1} + \frac{1}{C_2} = \frac{1}{C_1} + \frac{1}{C_1} = \frac{2}{C_1}$

$$C_1 = \frac{\epsilon_0 A}{\frac{d-a}{2}} = \frac{2\epsilon_0 A}{d-a}$$

$$C_{\text{eff}} = \frac{C_1}{2} = \frac{\epsilon_0 A}{d-a}$$

(b) $C_{\text{eff}} = \frac{\epsilon_0 A}{d} \cdot \frac{d}{d-a} = C_0 \frac{d}{d-a} = \frac{dC_0}{d-a}$

(c) $a \rightarrow 0 \quad C_{\text{eff}} \rightarrow \frac{dC_0}{d} \rightarrow C_0$ the very thin metal has no effect.

$$a \rightarrow d \quad C_{\text{eff}} \rightarrow \infty$$

For a given potential difference, Q is large when y is small