

HW Solution 5

October 4, 2010

35.50

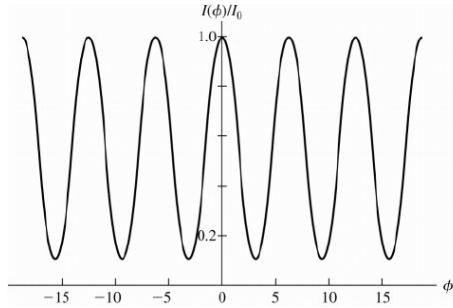
$$(a) E_p^2 = E_1^2 + E_2^2 - 2E_1E_2\cos(\pi - \phi) = E^2 + 4E^2\cos\phi = 5E^2 + 4E^2\cos\phi$$

$$I = \frac{1}{2}\delta_0cE_p^2 = \delta_0c\left[\left(\frac{5}{2}E^2\right) + \left(\frac{4}{2}E^2\right)\cos\phi\right]$$

$$\phi = 0 \Rightarrow I_0 = \frac{9}{2}\delta_0cE^2$$

$$\therefore I = I_0\left[\frac{5}{9} + \frac{4}{9}\cos\phi\right]$$

(b) The graph is shown in the figure. $I_{min} = \frac{1}{9}I_0$ which occurs when $\phi = n\pi$ (n odd).



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$$(a) I = \frac{1}{2}I_0 \text{ so } \frac{\sin\beta/2}{\beta/2} = \frac{1}{\sqrt{2}}$$

Let $x = \beta/2$, the equation for x is $\frac{\sin x}{x} = \frac{1}{\sqrt{2}} = 0.7017$

$$\therefore x = 1.39 \text{ rad}, \beta = 2.78 \text{ rad}$$

$$\Delta\theta = 2\theta_+, \sin\theta_+ = \frac{\lambda\beta}{2\pi a} = 0.4425\left(\frac{\lambda}{a}\right)$$

$$(i) \text{ For } \frac{a}{\lambda} = 2, \sin\theta_+ = 0.2212, \theta_+ = 12.78^\circ, \Delta\theta = 25.6^\circ$$

$$(ii) \text{ For } \frac{a}{\lambda} = 5, \sin\theta_+ = 0.0885, \theta_+ = 5.077^\circ, \Delta\theta = 10.2^\circ$$

$$(iii) \text{ For } \frac{a}{\lambda} = 10, \sin\theta_+ = 0.04425, \theta_+ = 2.536^\circ, \Delta\theta = 5.1^\circ$$

(b)

$$(i) \text{ For } \frac{a}{\lambda} = 2, \sin\theta_0 = \frac{1}{2}, \theta_0 = 30.0^\circ, 2\theta_0 = 60^\circ$$

$$(ii) \text{ For } \frac{a}{\lambda} = 5, \sin\theta_0 = \frac{1}{5}, \theta_0 = 11.54^\circ, 2\theta_0 = 23.1^\circ$$

$$(iii) \text{ For } \frac{a}{\lambda} = 10, \sin\theta_0 = \frac{1}{10}, \theta_0 = 5.74^\circ, 2\theta_0 = 11.5^\circ$$

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(a) $d\sin\theta = m\lambda$. Place 1st maximum at ∞ or $\theta = 90^\circ$. $d = \lambda$. If $d < \lambda$, this puts the first maximum "beyond ∞ ." Thus, if $d < \lambda$ there is only a single principal maximum.

(b) At a principal maximum when $\delta = 0$, the phase difference due to the path difference between adjacent slits is $\Phi_{path} = 2\pi\left(\frac{d\sin\theta}{\lambda}\right)$. This just scales 2π radians by the fraction the wavelength is of the path difference between adjacent sources. If we add a relative phase δ between sources, we still must maintain a total phase difference of zero to keep our principal maximum.

$$\Phi_{path} \pm \delta = 0 \Rightarrow \frac{2\pi d\sin\theta}{\lambda} = \pm\delta \text{ or } \theta = \sin^{-1}\left(\frac{\delta\lambda}{2\pi d}\right)$$

(c) $d = 0.02m$. Let $\theta = 45^\circ$. For $f\lambda = c$,

$$\delta_{max} = \pm \frac{2\pi(0.02m)(8.8 * 10^9 Hz) \sin 45^\circ}{3.00 * 10^8 m/s} = \pm 2.61 rad$$