

# HW Solution 13

November 30, 2010

## 41.36

(a)

For  $l = 3$ ,  $m_l = \pm 3, \pm 2, \pm 1, 0$  and  $m_s = \pm \frac{1}{2}$

For  $l = 2$ ,  $m_l = \pm 2, \pm 1, 0$  and  $m_s = \pm \frac{1}{2}$

For  $l = 1$ ,  $m_l = \pm 1, 0$  and  $m_s = \pm \frac{1}{2}$

(b)

For N shell  $n = 4$ . For an  $f$ -electron,  $l = 3$ .

$\therefore L = \sqrt{12}\hbar$ ,  $L_z = m_l\hbar = \pm 3, \pm 2, \pm 1, 0$  with maximum  $3\hbar$ ,  $S = \sqrt{3/4}\hbar$  for all electrons.

(c)

For  $d$ -state electron,  $l = 2$ ,  $L = \sqrt{6}\hbar$ ,  $L_z = m_l\hbar$  with maximum  $2\hbar$ .

$\cos\theta_{min} = \frac{L_z}{L} = \frac{2}{\sqrt{6}}$ ,  $\theta = 35.3^\circ$ .

$\cos\theta_{min} = -\frac{2}{\sqrt{6}}$ ,  $\theta = 144.7^\circ$ .

(d)

This is not possible since  $l = 3$  for an  $f$ -electron, but in the M shell the maximum value of  $l$  is 2.

## 41.50

(a)

The energy shift from zero field is  $\Delta U_0 = m_l\mu_B B$ .

For  $m_l = 2$ ,  $\Delta U_0 = 1.62 * 10^{-4} eV$ .

For  $m_l = 1$ ,  $\Delta U_0 = 8.11 * 10^{-5} eV$ .

(b)

$|\Delta\lambda| = \lambda \frac{|\Delta E|}{E_0}$ , where  $E_0 = 13.6 eV(1/4 - 1/9)$ ,  $\lambda_0 = 6.563 * 10^{-7} m$  and  $\Delta E = 1.62 * 10^{-4} - 8.11 * 10^{-5} = 8.09 * 10^{-5} eV$ .

$\therefore |\Delta\lambda| = 0.0281 nm$ .

The wavelength corresponds to a larger energy change, and so the wavelength is smaller.